## Rotation Angle of a Vertical Plane

## OBJECTIVE

This document describes how to measure the rotational angle around a horizontal axle.
Small inclinations are possible to measure accurately with one sensor, but when exceeding $30^{\circ}$, two sensors are usually required.

## DESCRIPTION OF APPLICATION

As the sensor is an accelerometer, the signal is linear with respect to the horizontal component of earth's gravity (=acceleration 1 g ), and sine shaped as a function of the tilt angle. By definition, the sensitivity will decrease when approaching $90^{\circ}$ (fig.1.)

Figure1.
Output in $g$ as a function of the tilt angle.


Close to $0^{\circ}$ the correlation between inclination in $g$ and angle is nearly linear (fig.2.), thus enabling the use of the sensors in without additional signal processing.

Figure2.
In the $\pm 30^{\circ}$ range nonlinearity is $0,5^{\circ}$.


For linearization, the output signal needs to be transformed by the arcsine function.

$$
\alpha=\arcsin (x), \text { where } \mathrm{x} \text { is the inclination in } \mathrm{g}
$$

However, the accuracy decreases the further away from 0 g one is, as does the sensitivity.


## RECOMMENDATION

For good inclination accuracy, a dual axis sensor should be used. The measuring axes should be orthogonal to each other, and perpendicular to the rotation axis. By definition, the signal is linear when calculated as follows:

$$
\alpha=\arctan \left(\frac{x}{y}\right), \text { where } \mathrm{x} \text { and } \mathrm{y} \text { are inclination in } \mathrm{g}
$$

Figure 3.
Linearized output signal by using dual axis sensor and arctan calculation.


## APPLICATIONS

The above solution enables linear measurement over a wide inclination range, for example the counterand clockwise rotation of a vertical plane.

| Angle | $0^{\circ}$ | 0...90 ${ }^{\circ}$ | $90^{\circ}$ | 90...180 ${ }^{\circ}$ | $180^{\circ}$ | 180...270 ${ }^{\circ}$ | $270^{\circ}$ | Dir. of gravity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| X-channel | Og | $0=>1 \mathrm{~g}$ | +1g | 1 => 0g | 0g | $0=>-1 \mathrm{~g}$ | -19 | $\downarrow$ |
| Y-channel | 1 g | $1=>0 \mathrm{~g}$ | 0 g | $0=>-1 \mathrm{~g}$ | -1g | $-1=>0 \mathrm{~g}$ | Og |  |
| Position (module) |  | 琞 |  | So | Be | en |  |  |

## SUITABLE VTI PRODUCTS

All VTI dual axis products with the measuring range $\geq 1 \mathrm{~g}\left(90^{\circ}\right)$ are suitable for this application. Parts available in the following series are: SCA1000, SCA100T, SCA121T, SCA124T, and SCA125T.

